

# Impulse

## Level 3 Physics

January 2013

# Recall from Last Time

## Momentum

$$p = m * v$$

Note that  $p$  is the symbol for momentum.

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## Momentum

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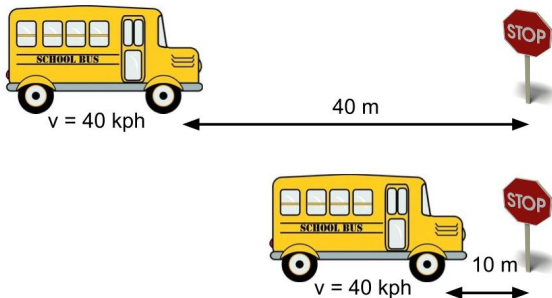
Note that  $p$  is the symbol for momentum.

## Conservation of Momentum

The net momentum of a system remains constant when there is no net force on the system.

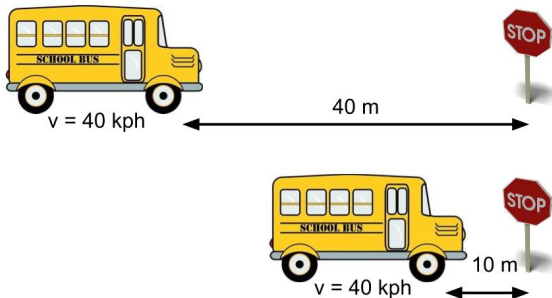
# Relating Momentum and Force

Consider these two situations of a school bus making a stop.



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It appears that given constant change in momentum, force and time are inversely related.

## Relating Momentum and Force

Make the assumption that mass and acceleration (and therefore force) are constant.

$$F = m * a$$

$$F = m * \frac{\Delta v}{\Delta t}$$

$$F = \frac{\Delta(m * v)}{\Delta t}$$

$$F = \frac{\Delta p}{\Delta t}$$

$$\Rightarrow \Delta p = F * \Delta t$$

# Impulse

## Definition

Impulse is the change in momentum. It is given by the formula

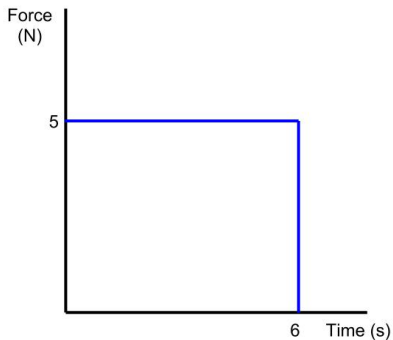
$$J = F * \Delta t = p_f - p_i$$

where force is constant.

Note that J is the symbol for impulse.

# Reading Graphs

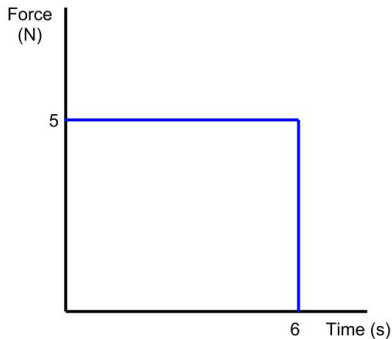
What is the impulse of a system undergoing change described by this graph?





# Reading Graphs

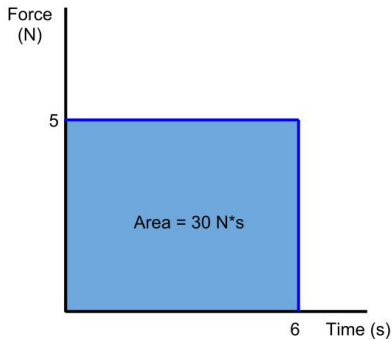
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$$\begin{aligned} J &= F * \Delta t \\ &= 5 * 6 \\ &= 30 N * s \end{aligned}$$

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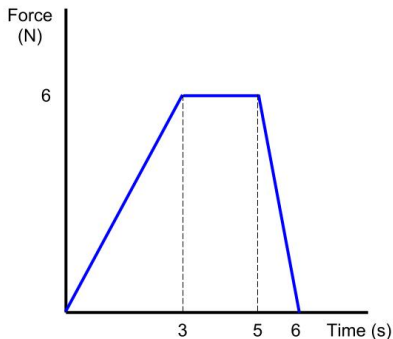
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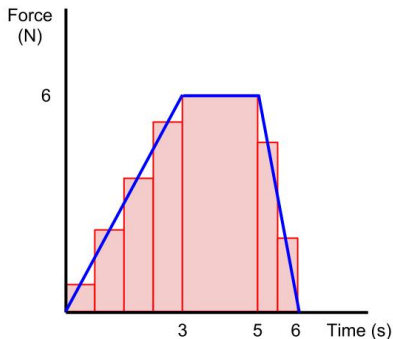
## More Complicated Graph

What is the impulse of a system undergoing change described by this graph?



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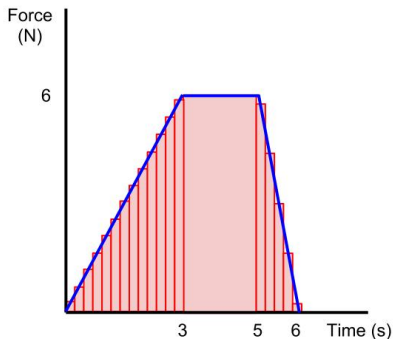
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Approximate the graph using segments of constant force

## More Complicated Graph

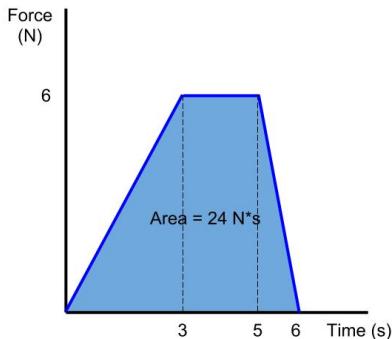
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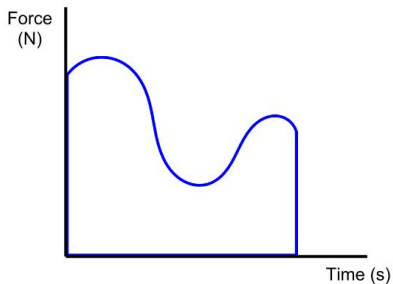
Approximate the graph using segments of constant force

**Impulse is the area under a force-time graph**

$$\begin{aligned} J &= \sum F * \Delta t \\ &= 0.5(6)(3) + 6(2) + 0.5(6)(1) \\ &= 9 + 12 + 3 \\ &= 24N * s \end{aligned}$$

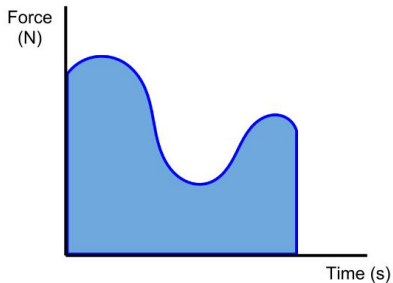
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Suppose there is a system that undergoes the change described by the graph below.



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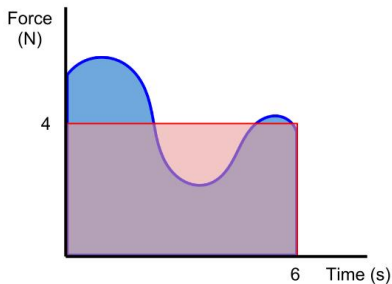


It is difficult to find the area



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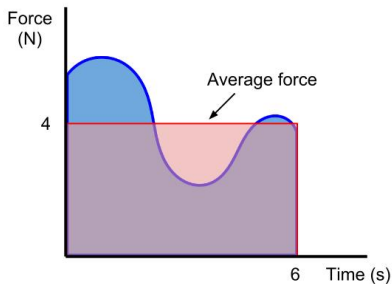


It is difficult to find the area

Suppose a horizontal line is drawn such that the area of the blue and pink regions are equal. What does the horizontal line represent?

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Suppose a horizontal line is drawn such that the area of the blue and pink regions are equal. What does the horizontal line represent? **Average force**

# Finding Averages

Why does finding a horizontal line that produces the same area give the average force?

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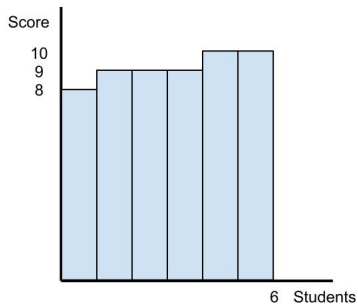
Let's consider a similar problem of finding the average of students' test scores.

Suppose 1 student gets 8/10, 3 students get 9/10, and 2 students get 10/10.

$$\begin{aligned}\text{avg. score} &= \frac{1(8) + 3(9) + 2(10)}{1 + 3 + 2} \\ &= \frac{55}{6} \\ &= 9.17\end{aligned}$$

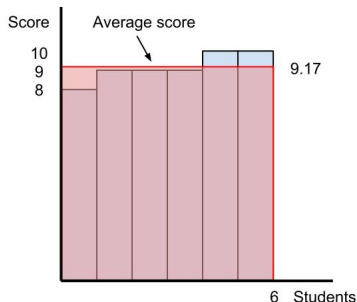
# Averages using Graphs

Now consider the test scores problem using a graph.



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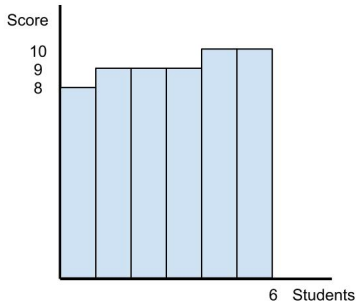


The calculation we did before is related to finding the area

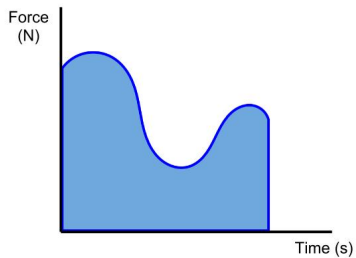
$$\begin{aligned}\text{avg. score} &= \frac{1(8) + 3(9) + 2(10)}{1 + 3 + 2} \\ &= \frac{\text{area of blue}}{\text{total students}}\end{aligned}$$

# Back to Average Force

## Test Scores

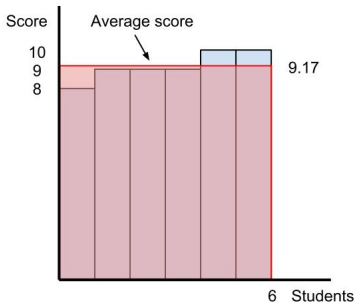


## Impulse



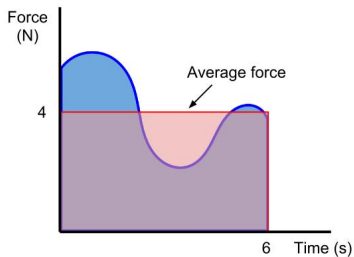
# Back to Average Force

## Test Scores



$$\text{avg. score} = \frac{\text{blue area}}{\text{total students}}$$

## Impulse



$$\text{avg. force} = \frac{\text{blue area}}{\text{total time}}$$



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## Average Force

Average force is given by the formula

$$\text{average force} = \frac{J}{\Delta t} = \frac{p_f - p_i}{\Delta t}$$

# Relevance

Why do we care about impulse and average force?

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Hint: The strongest bones in a human body can withstand up to 4000 N of force without breaking.

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Hint: Force and time are inversely related in the formula for average force.

# Pole Vaulting



The landing mat increases the time of impact, decreasing the average force the pole vaulter experiences.

# Boxing



Similarly, boxing gloves and helmets increase the time of impact, decreasing the average force experienced by the boxer.

# Gymnastics



Gymnasts are taught to land with their knees bent. This increases the time of impact, reducing the force on their lower body.



# Airbags



During car crashes, air bags inflate in order to increase the time of impact.

# Units

What are the units of impulse?

- 1  $\text{N}\cdot\text{s}$
- 2  $\text{kg}\cdot\text{m}/\text{s}$
- 3 Both  $\text{N}\cdot\text{s}$  and  $\text{kg}\cdot\text{m}/\text{s}$

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- 1 Magnitude
- 2 Direction
- 3 Magnitude and direction

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(Note that the direction of the impulse also tells you the direction of the average force.)

# Dough

A piece of dough with mass  $0.5 \text{ kg}$  is traveling downward at a speed of  $1 \frac{m}{s}$ . It lands on the table and sticks. If the coordinate system is defined such that up is positive, what is the impulse?

- 1  $0 \text{ N}\cdot\text{s}$
- 2  $0.5 \text{ N}\cdot\text{s}$
- 3  $-0.5 \text{ N}\cdot\text{s}$

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# Tennis ball

You throw a tennis ball with mass  $0.05\text{ kg}$  at the ground at a speed of  $2\frac{m}{s}$ . It makes contact with the ground for  $0.1$  seconds, and then the tennis ball bounces up at a speed of  $2\frac{m}{s}$ . What is the magnitude and direction of the average force experienced by the tennis ball?

- 1  $2\text{ N}$ , upward
- 2  $2\text{ N}$ , downward
- 3  $1\text{ N}$ , upward
- 4  $1\text{ N}$ , downward



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- 1 **2 N, upward**
- 2 2 N, downward
- 3 1 N, upward
- 4 1 N, downward